

Use a sum or difference identity to find the exact value for each expression.

1)  $\sin 195^\circ$

2)  $\cos \frac{11\pi}{12}$

3)  $\tan \frac{11\pi}{12}$

Use a half angle identity to find the exact value for each expression.

4)  $\sin \frac{5\pi}{8}$

5)  $\cos \frac{5\pi}{8}$

6)  $\tan \frac{5\pi}{8}$

Write the expression as the sine, cosine, or tangent of an angle.

7)  $\cos 94^\circ \cos 18^\circ + \sin 94^\circ \sin 18^\circ$

8)  $\sin \frac{\pi}{3} \cos \frac{\pi}{7} - \sin \frac{\pi}{7} \cos \frac{\pi}{3}$

Find each of the following when  $\sin x = \frac{2}{3}$  and  $\sin y = \frac{4}{5}$ .

9)  $\sin 2x$

10)  $\cos \frac{x}{2}$

11)  $\sin(x + y)$

12)  $\cos(x + y)$

**Prove each identity.**

$$13) \cos\left(x - \frac{\pi}{2}\right) = \sin x$$

$$14) \sin(\pi - x) = \sin x$$

$$15) \cos(x - y) + \cos(x + y) = 2 \cos x \cos y$$

$$16) \sin 4x + \sin 2x = 2 \sin 3x \cos x$$

$$17) (\sin x + \cos x)^2 = 1 + \sin 2x$$

$$18) 1 + \cos 10x = 2 \cos^2 5x$$

$$19) \sin 4x = 4 \sin x \cos x (1 - 2 \sin^2 x)$$

$$20) \cos x + 2 \sin^2 \frac{x}{2} = 1$$

Solve each equation on the interval  $[0, 2\pi)$ .

21)  $\cos 2x + \sin x = 1$

22)  $1 + \cos^2 x = 2 \cos^2 \frac{x}{2}$

23)  $\cos^2 x = \sin^2 \frac{x}{2}$

24)  $\sin 2x = \sin x$

25)  $2 \cos^2 x + \cos x = \cos 2x$

26)  $\sin \frac{x}{2} = -1$