

AP Calculus
3.4 Worksheet

All work must be shown in this course for full credit. Unsupported answers may receive NO credit.

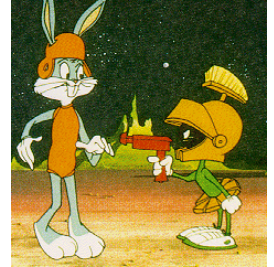
1. What is the relationship between position, velocity, and acceleration?

2. Once again trying to blow up earth because it interferes with his view of Venus, Marvin the Martian lands on the moon. Bugs Bunny, as always, interferes with his plan. Chasing Bugs, Marvin fires a warning shot straight up into the air with his Acme Disintegration Pistol. The height (in feet) after t seconds of the shot is given by

$$s(t) = -2.66t^2 + 135t + 3.$$

a) Find the velocity and acceleration as functions of time.
(What is the meaning of the acceleration function?)

b) What is the position of the shot when the velocity is 0?



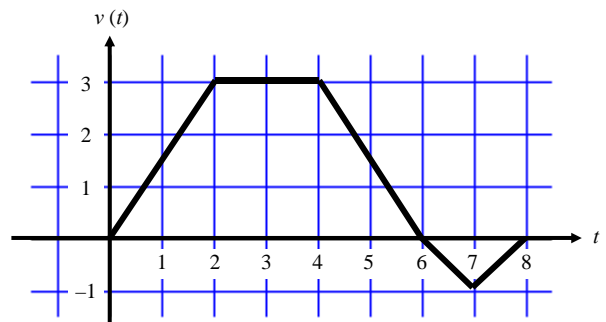
3. Fill in the blanks.

- a) When the _____ is positive, the object is moving in a positive direction.
- b) An object is _____ when the velocity and acceleration have different signs.
- c) An object is stopped when _____ is zero.
- d) Speed is always positive because it is the _____ of velocity.

4. A bug begins to crawl up a vertical wire at time $t = 0$. The velocity, v , of the bug at time t , $0 \leq t \leq 8$ is given by the function whose graph is shown below.

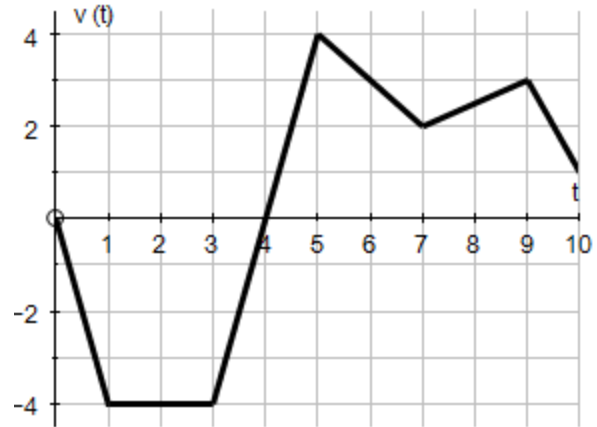
a) At what value of t does the bug change direction?
Justify your response.

b) During which time intervals in the bug slowing down?
Justify your response.



5. The figure graphed below shows the velocity of a particle moving along a coordinate line. Justify each response.

- a) When is the particle moving right?
- b) When is the particle moving left?
- c) When is the particle stopped?
- d) When is the particle speeding up?
- e) When does the particle change directions?
- f) When is the particle slowing down?
- h) When is the particle's acceleration positive?



- g) What is the particle moving at its greatest speed?
- i) When is the particle's acceleration negative?

6. Fill in the blanks with correct mathematical notation.

- a) If you want the average velocity of a particle on the interval $[2, 5]$, you must find _____.
- b) If you want the velocity of a particle at $t = 4$, you must find _____.

7. Velocity is the rate of change of _____. If the position of a particle on the x – axis at time t is given by $-5t^2$, then what is the average velocity of the particle for $0 \leq t \leq 3$?

8. A particle moves along the x – axis so that its position at time t is given by $x(t) = t^2 - 6t + 5$. For what value of t is the velocity of the particle zero?

9. Fill in the blanks with correct mathematical notation.

- a) If you want the average acceleration of a particle on the interval $[1, 3]$, you must find _____.
- b) If you want the acceleration of a particle at $t = 8$, you must find _____.

10. Rocket A has a positive velocity $v(t)$ after being launched upward from an initial height of 0 feet at time $t = 0$ seconds. The velocity of the rocket is recorded for selected values of t over the interval $0 \leq t \leq 80$ seconds as shown in the table below.

t (sec)	0	10	20	30	40	50	60	70	80
$v(t)$ (ft/sec)	5	14	22	29	35	40	44	47	49

a) Find the average acceleration of Rocket A over the time interval $0 \leq t \leq 80$ seconds. Indicate units of measure.

b) Using the data in the table, find an estimate for $v'(35)$. Indicate units of measure.

11. A particle moves along the x -axis so that its position at any time $t \geq 0$ is given by the function $x(t) = t^3 - 12t + 1$, where x is measured in feet and t is measured in seconds. Justify each response and indicate units of measure when appropriate.

a) Find the displacement during the first 3 seconds. b) Find the average velocity during the first 3 seconds.

c) Find the instantaneous velocity at $t = 3$ seconds. d) Find the acceleration when $t = 3$ seconds.

e) When is the particle moving left? f) At what value(s) t does the particle change direction?

g) When is the particle speeding up?

13. [Calculator] The cost involved in maintaining annual inventory for a certain manufacturer is given by

$C(x) = \frac{1,008,000}{x} + 6.3x$, where x is the number of items stored. Find the marginal cost of storing the 351st item.