

1. Simplify each expression.

a) $\sin x(\cot x + \tan x)$

b) $\tan^2 x \cos^2 x + \cot^2 x \sin^2 x$

c) $\frac{1 + \sin \theta}{\cos \theta} + \frac{\cos \theta}{1 + \sin \theta}$

d) $\frac{\sec x}{\cos x} - \frac{\tan x}{\cot x}$

e) $\frac{\sin x + \tan x}{1 + \sec x}$

f) $\sec x - \tan x \sin x$

2. Prove each identity (5.1-5.2)

a) $2 - \sec^2 z = 1 - \tan^2 z$

b) $\sec x - \cos x = \sin x \tan x$

c) $\sec^2 x \tan^2 x + \sec^2 x = \sec^4 x$

d) $\cot \beta + \tan \beta = \frac{\sec^2 \beta}{\tan \beta}$

e) $\cos^2 x - \sin^2 x = 2 \cos^2 x - 1$

f) $\frac{\cos x - \cos y}{\sin x + \sin y} + \frac{\sin x - \sin y}{\cos x + \cos y} = 0$

g) $\frac{\cos \phi}{1 - \sin \phi} = \frac{1 + \sin \phi}{\cos \phi}$

h) $\frac{1 + \cos x}{\sin x} = \csc x + \cot x$

3. Prove each identity (5.3-5.4)

a) $\cos\left(x - \frac{\pi}{2}\right) = \sin x$

b) $\tan\left(x - \frac{\pi}{2}\right) = -\cot x$

c) $\cos(x - y) + \cos(x + y) = 2 \cos x \cos y$

d) $\sin 4x + \sin 2x = 2 \sin 3x \cos x$

e) $(\sin x + \cos x)^2 = 1 + \sin 2x$

f) $1 + \cos 10x = 2 \cos^2 5x$

g) $\sin 4x = 4 \sin x \cos x (1 - 2 \sin^2 x)$

h) $\cos x + 2 \sin^2 \frac{x}{2} = 1$

i) $\cos^3 x = \frac{1}{2} \cos x (1 + \cos 2x)$

4. Use a sum or difference identity to find the exact value for each expression.

a) $\cos 75^\circ$

b) $\sin 195^\circ$

c) $\cos \frac{11\pi}{12}$

d) $\tan \frac{11\pi}{12}$

5. Use a half angle identity to find the exact value for each expression.

a) $\sin \frac{5\pi}{8}$

b) $\cos \frac{5\pi}{8}$

c) $\sin \frac{5\pi}{12}$

6. Write the expression as the sine, cosine, or tangent of an angle.

a) $\sin \frac{\pi}{3} \cos \frac{\pi}{7} - \sin \frac{\pi}{7} \cos \frac{\pi}{3}$

b) $\cos 7y \cos 3y - \sin 7y \sin 3y$

7. Solve each equation on the interval $[0, 2\pi)$.

a) $2 \cos^2 x - 5 \cos x + 2 = 0$

b) $2 \cos^2 x = -\cos x$

c) $\tan^2 x + \tan x = 0$

d) $\cos 2x + \sin x = 1$

e) $1 + \cos^2 x = 2 \cos^2 \frac{x}{2}$

f) $\cos^2 x = \sin^2 \frac{x}{2}$

g) $\sin \frac{x}{2} + \cos x = 1$

h) $\sin 2x = \sin x$